

# ARYAN INSTITUTE

CLASS-11<sup>TH</sup>  
SUBJECT-MATHS  
SAMPLE PAPER -01

TIME:3hr

M:M-80

**General Instructions:**

1. All questions are compulsory. There are 36 questions in all.
2. This question paper has four sections: Section A, Section B, Section C and Section D.
3. Section A contains twenty questions of one mark each, Section B contains six questions of two marks each, Section C contains six questions of four marks each, and Section D contains four questions of six marks each.
4. There is no overall choice. However, internal choices have been provided in three questions of 1 mark each, two questions of 2 marks each, two questions of 4 marks each, and two question of 6 marks each. You have to attempt only one of the alternatives in all such question.
5. Use of calculates is not permitted.

**SECTION-A**

- Q1.** Let S be the set of all real numbers. Then the relation  $R = \{(a, b): 1 + ab > 0\}$  on S is
- (a) reflexive symmetric and transitive
  - (b) reflexive and symmetric but not transitive
  - (c) reflexive and transitive but not symmetric
  - (d) symmetric and transitive but nor reflexive
- Q2.** In an examination, a candidate is required to pass at lest four different subjects out of 6. Then the number of ways in which he can fail is
- (a) 12                      (b) 16                      (c) 24                      (d) 42
- Q3.** Find a if the coefficient of  $x^2$  and  $x^3$  in the expansion of  $(3 + ax)^9$  are equal
- (a)  $\frac{8}{5}$                       (b)  $\frac{9}{5}$                       (c)  $\frac{8}{7}$                       (d)  $\frac{9}{7}$
- Q4.** Number of divisors of  $n = 38808$  (except 1 and  $n$ ) is
- (a) 74                      (b) 70                      (c) 68                      (d) 72
- Q5.** In Z, the set of all integer, inverse of  $-7$  w.r.t.  $*$ , defined by  $a * b = a + b + 7$  for all  $a, b \in Z$ , is
- (a) -14                      (b) 14                      (c) -7                      (d) 7
- Q6.** If  $x^n - 1$  is divisible by  $x - k$  for all  $n$  belong to naturals N, then the least

positive integral value of k is:

- (a) 4                      (b) 3                      (c) 1                      (d) 2

**Q7.** A sum of money is rounded off to the nearest rupee. The probability that the error occurred in rounding of is at least 15 paise is

- (a)  $\frac{29}{101}$                       (b)  $\frac{29}{100}$                       (c)  $\frac{71}{101}$                       (d)  $\frac{71}{100}$

**Q8.** The points A (5, -1, 1), B (7, -4, 7), C (1, -6, 10) and D (-1, -3, 4) are the vertices of

- (a) square                      (b) rhombus                      (c) none of these                      (d) rectangle

**Q9.** Five letters are sent to different person and addresses on the five envelopes are written at random. The probability that all the letters reach correct density is

- (a) none of these                      (b)  $\frac{44}{120}$                       (c)  $\frac{1}{5}$                       (d)  $\frac{1}{120}$

**Q10.** In the expansion of  $(1 + x)^{60}$ , the sum of coefficients of odd powers of x is

- (a)  $2^{58}$                       (b)  $2^{60}$                       (c)  $2^{61}$                       (d)  $2^{59}$

**Q11.** If  $f(1 + x) = x^2 + 1$ , then  $f(2 - h)$  is.....

**Q12.** Fill in the blanks:

The coefficient of  $x^5$  on the expansion  $(x+3)^8$  is.....

**Q13.** The continued product of first n natural numbers, is called the.....

**Q14.** Fill in the blanks:

The plane parallel to yz-plane is perpendicular to.....

**OR**

If the point P lies on z-axis, then coordinates of P are of the form.....

**Q15.** The value of the limit:  $\lim_{z \rightarrow 3} x + 3$  is .....

**OR**

The value of limit  $\lim_{z \rightarrow 0} \frac{\sin ax}{bx}$  is .....

**Q16.** If  $A = \{3, 5, 7, 9, 11\}$ ,  $B = \{7, 9, 11, 13\}$ ,  $C = \{11, 13, 15\}$  and  $D = \{15, 17\}$   
find:  $(A \cap B) \cap (B \cup C)$

**Q17.** How many natural numbers less than 1000 can be formed with the digits 1,2,3,4 and 5, if repetition of digits is allowed?

**Q18.** Find the product of complex numbers  $(2 + 9i)$ ,  $(11 + 3i)$ .

**OR**

Express  $(\sin 130^\circ - i \cos 135^\circ)$  in polar form.

**Q19.** If  $U = \{1, 2, 3, 4\}$  and  $R = \{(x, y): y > x \text{ for all } x, y \in U\}$ , then find the domain and range of R.

- Q20.** In how many ways, can a cricket team of 11 players be selected out of 16 players, If two particular players are always to be included?
- Q21.** In a school, there are 20 teachers who teach mathematics or physics. Of these, 12 teach mathematics and 4 teach physics and mathematics. How many teach physics

**OR**

Find  $A \Delta B$ , if  $A = \{1, 3, 4\}$  and  $B = \{2, 5, 9, 11\}$ .

- Q22.** Two die are thrown together. What is the probability that the sum of the number on the two faces is either divisible by 3 or by 4?
- Q23.** Find the term independent of  $x$  in the expansion of  $\left(3x - \frac{2}{x^2}\right)^{15}$ .
- Q24.** Without using Pythagoras theorem, show that (12, 8), (-2, 6) and (6,0) are the vertices of right-angled triangle.

**OR**

Find the slope of a line, which passes through the origin and mid-point of the line segment joining the points P(0, -4) and B (8, 0).

- Q25.** Given below are two statements  
P : 25 is a multiple of 5  
Q :25 is multiple of 8  
Write the compound. Statements connecting these two statements with “and” and “or”. In both cases check the validity of the compound statement.
- Q26.** Solve :  $\sin 2x + \cos x = 0$ .
- Q27.** In a survey of 25 students, it was found that 15 had taken mathematics, 12 had taken physics and 11 had taken chemistry, 5 had taken mathematics and chemistry, 9 had taken mathematics and physics, 4 had taken physics and chemistry and 3 had taken all the three subjects. Find the number of students who had none of the subjects.
- Q28.** Let  $A = \{1, 2, 3, 4\}$ ,  $B = \{1,5,11,15,16\}$  and  $f = \{(1,5), (2,9), (3,1), (4,5), (2,11)\}$ . Are the following true?  
(i)  $f$  is a relation from A to B.  
(ii)  $f$  is a function from A to B. Justify.

**OR**

Find the domain and the range of the real function  $f$  defined by  $f(x) = |x-1|$ .

- Q29.** Find the derivative of the following functions (it is to be understood that a, b, c, d, p, q, r and s are fixed non-zero constants and m and n are integer):  
 $(ax+b)(cx+d)^2$
- Q30.** Solve the equation  $25x^2 - 30x + 11 = 0$  by using the general expression for the roots of a quadratic equation and show that the roots are complex conjugate.

- Q31.** Solve the following system of inequalities graphically:  
 $x + y \leq 9, y > x, x \geq 0$

**OR**

Solve the inequalities graphically in two-dimensional plane:  $-3x + 2y \geq -6$

- Q32.** Use the principle of Mathematics Induction to prove that  $n^3 + 3n^2 + 5n + 3$  is divisible by 3, for all-natural number n.

- Q33.** Prove that  $\cos^3 A + \cos^3(120^\circ + A) + \cos^3(240^\circ + A) = \frac{3}{4} \cos^3 A$ .

**OR**

If  $x \cos \theta = y \cos \left( \theta + \frac{2\pi}{3} \right) = z \cos \left( \theta + \frac{4\pi}{3} \right)$ , then show that  $xy + yz + zx = 0$ .

- Q34.** Find the sum to n terms in each of the series  $3 \times 1^2 + 5 \times 2^2 + 7 \times 3^2 + \dots$

- Q35.** Find the equation of the ellipse whose foci are (6, 4) and (-4, 4) and eccentricity is 2.

**OR**

Find the equation of the ellipse, whose foci are  $(\pm 3, 0)$  and passing through (4, 1).

- Q36.** An original frequency table with mean 11 and variance 9.9 was lost but the following table derived from it was found. Construct the original table.

<b>Value of deviation (d)</b>	-2	-1	0	1	2
<b>Frequency (f)</b>	1	6	7	4	2